

Package ‘phylocurve’

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Description phylocurve offers a variety of phylogenetic comparative tools for studying the evolution of function-valued traits (as well as other high-dimensional traits) including ancestral state reconstruction, estimating phylogenetic signal, and assessing correlated trait evolution. Visit <http://www.phylocurve.org> for more information.

License GPL (>= 2)

URL <http://www.phylocurve.org>

Imports ape, geiger, phytools, abind, phylolm

R topics documented:

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phylocurve-package	<i>phylocurve: Phylogenetic comparative methods for function-valued and other high-dimensional traits</i>
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Description

phylocurve offers a variety of phylogenetic comparative tools for studying the evolution of function-valued traits (as well as other high-dimensional traits) including ancestral state reconstruction, estimating phylogenetic signal, and assessing correlated trait evolution.

Details

Package: phylocurve
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Version: 1.0.0
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Author(s)

Eric W. Goolsby <eric.goolsby.evolution@gmail.com>

References

Goolsby, E.W. 2015. "Phylogenetic comparative methods for evaluating the evolutionary history of function-valued traits." *Systematic Biology*. In press.

Adams, D.C. 2014. A method for assessing phylogenetic least squares models for shape and other high-dimensional multivariate data. *Evolution*. 68:2675-2688.

Adams, D.C. 2014. A generalized K statistic for estimating phylogenetic signal from shape and other high-dimensional multivariate data. *Systematic Biology*. 63:685-697.

Ho, L. S. T. and Ane, C. 2014. "A linear-time algorithm for Gaussian and non-Gaussian trait evolution models". *Systematic Biology* 63(3):397-408.

Examples

```
require(phytools)

# simulate evolution of a function-valued trait (glm with logit link)
sim_data <- sim.curves()

# perform ancestral curve reconstruction
anc_recon <- phylocurve(y~x, tree = sim_data$tree, data = sim_data$data)

# get tip coefficients and aligned function data
tip_coefficients <- get_tip_coefficients(formula = y~x, tree = sim_data$tree, data = sim_data$data)
data <- get_aligned_function_data(tip_coefficients)
```

```
# estimate evolutionary rates
rate.mult.fitted <- rate.mult(sim_data$tree,data)

# estimate phylogenetic signal
K.mult(rate.mult.fitted = rate.mult.fitted)
```

```
compare.multivar.rate.mult
```

Compare multiple multivariate evolutionary rates

Description

Compares hypotheses about evolutionary rates for multivariate traits combining methods from Adams (2013) and Adams (2014), using a covariance-based approach as described in Goolsby (2015).

Usage

```
compare.multivar.rate.mult(null_model, alt_model_list)
```

Arguments

`null_model` A fitted `rate.mult` object in which all data is fit under the null hypothesis (e.g., all traits fit under the same evolutionary rate).

`alt_model_list` A fitted `rate.mult` object in which all data is fit under the alternative hypothesis (e.g., traits are fit under different evolutionary rates).

Value

<code>null.logL</code>	Log-likelihood of the null model
<code>null.pars</code>	Number of parameters used to fit the null model
<code>alt.logL</code>	Log-likelihood of the alternative model
<code>alt.pars</code>	Number of parameters used to fit the alternative model
<code>df</code>	Degrees of freedom for likelihood ratio test
<code>chi_sq</code>	Chi-square value for likelihood ratio test
<code>p</code>	p-value for likelihood ratio test

Author(s)

Eric W. Goolsby

References

Adams D.C. 2013. Comparing evolutionary rates for different phenotypic traits on a phylogeny using likelihood. *Systematic Biology*. 62:181-192.

Adams D.C. 2014. Quantifying and comparing phylogenetic evolutionary rates for shape and other high-dimensional phenotypic data. *Systematic Biology*. 63:166-177.

Golsby E.W. 2015. Covariance-based maximum likelihood estimation is equivalent to and more flexible than distance-based phylogenetic comparative methods for high-dimensional multivariate traits. In review.

See Also

[rate.mult](#), [compare.rate.mult](#), [compare.evol.rates](#)

Examples

```
# Simulate random data for 2 multivariate traits
# (5 dimensions each) with different evolutionary rates
s <- sim.mult(nspecies = 50, R = diag(c(rep(1,5),c(rep(2,5))))))

# Estimate the null model (a single rate parameter)
null <- rate.mult(tree = s$tree, Y = s$Y_means)

# Estimate components of the alternative hypothesis and store in a list
alt1 <- rate.mult(s$tree, Y = s$Y_means[,c(1,2:6)])
alt2 <- rate.mult(s$tree, Y = s$Y_means[,c(1,7:11)])
alt_list <- list(alt1, alt2)

# Compare the null to the alternative to hypothesis
comparison <- compare.multivar.rate.mult(null_model = null, alt_model_list = alt_list)
```

compare.rate.mult *Compare evolutionary rates*

Description

This function tests for differences in evolutionary rates (and optionally, evolutionary models) using the methods described in Adams (2014) and Goolsby (2015) in a covariance-based approach.

Usage

```
compare.rate.mult(rate.mult.fitted, groups, fit_individual = FALSE)
```

Arguments

rate.mult.fitted A fitted `rate.mult` object in which all data is fit under the null hypothesis (e.g., all trait dimensions fit under the same evolutionary rate and/or evolutionary model).

groups A named factor by species specifying which group to assign individual species. For example, given a tree with 16 species, the command `setNames(object = factor(c(rep("a",8),rep("b",8)),levels=c("a","b")),nm = tree$tip.label)` assigns 8 species to group "a" and 8 species to group "b".

fit_individual Whether or not to fit individual evolutionary models to each trait dimension (if TRUE), or if a single evolutionary model is fit to all trait dimensions (if FALSE, the default). Ignored if `model="BM"`.

Value

null.logL Log-likelihood of the null model

null.pars Number of parameters used to fit the null model

alt.logL Log-likelihood of the alternative model

alt.pars Number of parameters used to fit the alternative model

df	Degrees of freedom for likelihood ratio test
chi_sq	Chi-square value for likelihood ratio test
p	p-value for likelihood ratio test
null_model_list	List of fitted rate.mult objects for the null model corresponding to each group
alt_model_list	List of fitted rate.mult objects for the alternative model corresponding to each group

Author(s)

Eric W. Goolsby

References

Adams D.C. 2014. Quantifying and comparing phylogenetic evolutionary rates for shape and other high-dimensional phenotypic data. *Systematic Biology*. 63:166-177.

Golsby E.W. 2015. Covariance-based maximum likelihood estimation is equivalent to and more flexible than distance-based phylogenetic comparative methods for high-dimensional multivariate traits. In review.

See Also

[rate.mult](#), [compare.multivar.rate.mult](#), [compare.evol.rates](#)

Examples

```
# Simulate random data for a multivariate trait with 50 species and 10 trait dimensions
s <- sim.mult(nspecies = 50,R = diag(10))

# Estimate the null model (a single rate parameter for the entire tree)
null <- rate.mult(tree = s$tree,Y = s$Y_means)

# Set 2 groups of species to test for different evolutionary rates
groups <- setNames(factor(c(rep("a",25),rep("b",25)),levels=c("a","b")),s$tree$tip.label)

# Test the hypothesis of different evolutionary rates for each group
compare.rate.mult(rate.mult.fitted = null,groups = groups)
```

get_aligned_function_data

Estimate aligned data for function-valued traits

Description

Estimates function data for tip species curves from tip coefficients.

Usage

```
get_aligned_function_data(tip_coefficients, ylength, ymin = 0.01, ymax = 0.99)
```

Arguments

tip_coefficients	Matrix of estimated regression coefficients of tip curves. Row names should correspond to species names. The first column should contain the logit glm intercept; the second column contains the logit glm slope.
ylength	How many landmarks (points on the curve) to evaluate.
ymin	Because 0 and 1 are undefined for inverse logit functions, the minimum and maximum values are defaulted to .01 and .99. Can be adjusted as needed.
ymax	Because 0 and 1 are undefined for inverse logit functions, the minimum and maximum values are defaulted to .01 and .99. Can be adjusted as needed.

Value

A data frame of aligned X-coordinates for function-valued traits for a given constant Y.

Author(s)

Eric W. Goolsby

References

Goolsby, E.W. 2015. "Phylogenetic comparative methods for evaluating the evolutionary history of function-valued traits." *Systematic Biology*. In press.

Examples

```
require(phytools)

# simulate evolution of a function-valued trait (glm with logit link)
sim_data <- sim.curves()

# get tip coefficients and aligned function data
tip_coefficients <- get_tip_coefficients(formula = y~x, tree = sim_data$tree, data = sim_data$data)
data <- get_aligned_function_data(tip_coefficients)

# estimate evolutionary rates
rate.mult.fitted <- rate.mult(sim_data$tree, data)

# estimate phylogenetic signal
K.mult(rate.mult.fitted = rate.mult.fitted)
```

get_tip_coefficients *Estimate regression coefficients for tip species curves*

Description

Estimates regression coefficients for tip species curves from raw data. May be useful if wanting to perform methods without first performing ancestral curve reconstruction via the phylocurve() function.

Usage

```
get_tip_coefficients(formula, tree, data, ymin = 0.01, ymax = 0.99,  
  ylength = 30, species_identifier = "species", verbose = FALSE)
```

Arguments

formula	Formula for function-valued trait (currently only supports models of the form $Y \sim X$)
tree	A phylogenetic tree of class "phylo"
data	A data frame with data for tip curve estimation, where each row contains a single data point. A column named "species" has the species names corresponding to each data point, a predictor (X) variable and the response (Y) variable, which must be scaled between 0 and 1.
ymin	Because 0 and 1 are undefined for inverse logit functions, the minimum and maximum values are defaulted to .01 and .99. Can be adjusted as needed.
ymax	Because 0 and 1 are undefined for inverse logit functions, the minimum and maximum values are defaulted to .01 and .99. Can be adjusted as needed.
ylength	How many landmarks (points on the curve) to evaluate.
species_identifier	Default is "species". Can be changed if the column in data has a different species identifier name.
verbose	either to print progress during tip curve coefficient estimation.

Value

Estimated regression coefficients of tip curves.

Examples

```
require(phytools)  
  
# simulate evolution of a function-valued trait (glm with logit link)  
sim_data <- sim.curves()  
  
# get tip coefficients and aligned function data  
tip_coefficients <- get_tip_coefficients(formula = y~x, tree = sim_data$tree, data = sim_data$data)  
data <- get_aligned_function_data(tip_coefficients)  
  
# estimate evolutionary rates  
rate.mult.fitted <- rate.mult(sim_data$tree, data)  
  
# estimate phylogenetic signal  
K.mult(rate.mult.fitted = rate.mult.fitted)
```

K.mult *Multivariate phylogenetic signal*

Description

Estimates multivariate phylogenetic signal (Adams 2014) using a covariance-based implementation (Goolsby 2015).

Usage

```
K.mult(rate.mult.fitted, iter = 1000)
```

Arguments

rate.mult.fitted	A fitted rate.mult object
iter	Number of phylogenetic permutations for significance testing

Value

phy.signal	Multivariate phylogenetic signal (Kmult)
pvalue	Significance of Kmult

Author(s)

Eric W. Goolsby

References

Adams, D.C. 2014. A generalized K statistic for estimating phylogenetic signal from shape and other high-dimensional multivariate data. *Systematic Biology*. 63:685-697.

Goolsby E.W. 2015. Covariance-based maximum likelihood estimation is equivalent to and more flexible than distance-based phylogenetic comparative methods for high-dimensional multivariate traits. In review.

See Also

[physignal](#)

Examples

```
# Simulate random data for a multivariate trait with 50 species and 10 trait dimensions
s <- sim.mult(nspecies = 50,R = diag(10))

# Estimate evolutionary rates
rate.mult.fitted <- rate.mult(tree = s$tree,Y = s$Y_means)

# Estimate multivariate phylogenetic signal
K.mult(rate.mult.fitted = rate.mult.fitted)
```

`pgls.mult`*Multivariate phylogenetic generalized least squares*

Description

Performs phylogenetic generalized least squares using the method described in Adams (2014) using a covariance-based approach (Goolsby 2015)

Usage

```
pgls.mult(rate.mult.fitted, X)
```

Arguments

`rate.mult.fitted`

A fitted `rate.mult` object

`X`

A matrix of predictor variables `X` for PGLS. Note, an intercept is estimated automatically (do not add a column of ones to `X`). Rows should be named according to species names.

Value

An object of class "anova"

Author(s)

Eric W. Goolsby

References

Adams, D.C. 2014. A method for assessing phylogenetic least squares models for shape and other high-dimensional multivariate data. *Evolution*. 68:2675-2688.

Goolsby E.W. 2015. Covariance-based maximum likelihood estimation is equivalent to and more flexible than distance-based phylogenetic comparative methods for high-dimensional multivariate traits. In review.

See Also

[procD.pgls](#)

Examples

```
# Simulate random data for a multivariate trait with 50 species and 10 trait dimensions
s <- sim.mult(nspecies = 50,R = diag(10))
```

```
# Simulate a univariate trait
require(phytools)
X <- as.matrix(fastBM(s$tree))
```

```
# Estimate evolutionary rates
rate.mult.fitted <- rate.mult(tree = s$tree,Y = s$Y_means)
```

```
# Perform multivariate phylogenetic regression
pgls.mult(rate.mult.fitted = rate.mult.fitted,X = X)
```

 phylocurve

Ancestral curve reconstruction

Description

This function performs ancestral reconstruction of function-valued traits. Currently only logistic regression (glm with logit link) is implemented.

Usage

```
phylocurve(formula, tree, data, ymin = 0.01, ymax = 0.99, ylength = 30,
  tip_coefficients, species_identifier = "species", verbose = FALSE)
```

Arguments

formula	Formula for function-valued trait (currently only supports models of the form $Y \sim X$)
tree	An phylogenetic tree of class "phylo"
data	A data frame with data for tip curve estimation, where each row contains a single data point. A column named "species" has the species names corresponding to each data point, a predictor (X) variable and the response (Y) variable, which must be scaled between 0 and 1.
ymin	Because 0 and 1 are undefined for inverse logit functions, the minimum and maximum values are defaulted to .01 and .99. Can be adjusted as needed.
ymax	Because 0 and 1 are undefined for inverse logit functions, the minimum and maximum values are defaulted to .01 and .99. Can be adjusted as needed.
ylength	How many landmarks (points on the curve) to evaluate.
tip_coefficients	A matrix of regression coefficients can be provided instead of raw data. Row names should be species names, the first column should be the glm logit intercept parameter, and the second column should be the glm logit slope parameter.
species_identifier	Default is "species". Can be changed if the column in data has a different species identifier name.
verbose	Whether to print progress during ancestral curve reconstruction.

Details

This function uses a PGLS-based method described in Goolsby (2015) to perform ancestral curve reconstruction. This function uses a fast tree transversal method via the phylolm package (Ho and Ane, 2014)

Value

node_coefficients	Estimated regression coefficients of internal nodes
fitted_x	Reconstructed x-values for each internal node. Curve coordinates for internal node <i>i</i> are (fitted_x[<i>i</i>],y_vals)
lower_CI_x	Lower 95 percent confidence interval for fitted x-values for each internal node
upper_CI_x	Upper 95 percent confidence interval for fitted x-values for each internal node
y_vals	Vector of y-values used as inputs for inverse function evaluation. Curve coordinates for internal node <i>i</i> are (fitted_x[<i>i</i>],y_vals)
tip_coefficients	Estimated regression coefficients of tip curves.

Author(s)

Eric W. Goolsby

References

- Goolsby, E.W. 2015. "Phylogenetic comparative methods for evaluating the evolutionary history of function-valued traits." *Systematic Biology*. In press.
- Ho, L. S. T. and Ane, C. 2014. "A linear-time algorithm for Gaussian and non-Gaussian trait evolution models". *Systematic Biology* 63(3):397-408.

Examples

```
require(phytools)

# simulate evolution of a function-valued trait (glm with logit link)
sim_data <- sim.curves()

# perform ancestral curve reconstruction
anc_recon <- phylocurve(y~x,tree = sim_data$tree,data = sim_data$data)

# get tip coefficients and aligned function data
tip_coefficients <- get_tip_coefficients(formula = y~x,tree = sim_data$tree,data = sim_data$data)
data <- get_aligned_function_data(tip_coefficients)

# estimate evolutionary rates
rate.mult.fitted <- rate.mult(sim_data$tree,data)

# estimate phylogenetic signal
K.mult(rate.mult.fitted = rate.mult.fitted)
```

print.rate.mult

Print rate.mult

Description

Generic S3 method for rate.mult

Usage

```
## S3 method for class 'rate.mult'
print(x, ...)
```

Arguments

x	An object of class rate.mult
...	Further arguments passed to or from other methods.

rate.mult

Estimate multivariate evolutionary rates and models

Description

This function estimates multivariate evolutionary rates (Adams 2014) and alternative evolutionary models using a covariance-based approach (Goolsby 2015). The function must be run prior to running other multivariate functions, including K.mult, pgl.s.mult, compare.rate.mult, and compare.multivar.rate.mult.

Usage

```
rate.mult(tree = tree, Y = Y, type = c("mult", "diag", "all"),
method = c("REML", "ML"), error = c("none", "estimate", "supply"),
error_n = 20, error_supply, model = "BM", fixed_sigma2, fixed_model_pars)
```

Arguments

tree	An object of class phylo
Y	A data frame in which the first column is labeled "species", and is filled with species names. The remaining columns contain values for the multivariate trait Y. Multiple observations per species (using multiple rows) and missing data are allowed.
type	The form of evolutionary rate estimation to use. If type="mult", a single evolutionary rate is estimated for all trait dimensions. If type="diag", a separate evolutionary rate is estimated for all trait dimensions. NOTE: the option type="all" is also available, in which an entire covariance matrix R is estimated for traits (not compatible with other functions!), in which case, only BM evolution with no missing data and no within-species error is allowed.
method	Whether to use restricted maximum likelihood (REML, the default) or maximum likelihood.
error	Whether to incorporate within-species measurement error. Can be set to "none" (the default) if only a single observation is available per species. If raw data with multiple observations per species is supplied, select "estimate" to estimate pooled within-species variance for species with less than error_n observations (for species with >error_n observations, variance is used). Alternatively, a matrix of the square of standard errors (variance divided by the number of within-species observations) for each species and trait dimension can be supplied if error is set to "supply".

error_n	Only relevant if error="estimate". For trait dimensions with less than error_n within-species observations, pooled within-species variance is used. If the number of within-species observations for a trait dimension is greater than or equal to error_n, variance is estimated directly.
error_supply	Only relevant if error="supply". A matrix of species and trait dimension squared standard errors (or variance divided by the number of within-species observations). Row names should be species names.
model	Evolutionary model specification – default is "BM". Other options include "OUrandomRoot", "OUfixedRoot", "EB", "lambda", "kappa", and "delta". More than one model may be specified (e.g., c("lambda","EB")), in which case the branch length transformations are applied in order of the specified models. NOTE: if incorporating alternative models, DO NOTE include "BM".
fixed_sigma2	If the evolutionary rate (single value if type="mult") or rates (if type="diag") is desired to be fixed, entire it here.
fixed_model_pars	If the evolutionary model parameter or parameters are desired to be fixed, entire them here in a vector named according to the appropriate model (should be in order of the models specified by the model argument).

Value

sigma2	Estimated evolutionary rate
pars	Estimated evolutionary model parameters (NULL If model="BM")
logL	Log-likelihood of the estimated parameters
method	REML or ML
model	Evolutionary model
rate.mult.args	List of arguments to be called with do.call(rate.mult,rate.mult\$rate.mult.args)

Author(s)

Eric W. Goolsby

References

- Adams D.C. 2014. Quantifying and comparing phylogenetic evolutionary rates for shape and other high-dimensional phenotypic data. *Systematic Biology*. 63:166-177.
- Goolsby E.W. 2015. Covariance-based maximum likelihood estimation is equivalent to and more flexible than distance-based phylogenetic comparative methods for high-dimensional multivariate traits. In review.

See Also

[compare.multivar.rate.mult](#), [compare.rate.mult](#), [compare.evol.rates](#)

Examples

```
# Simulate random data for a multivariate trait with 50 species and 10 trait dimensions
s <- sim.mult(nspecies = 50,R = diag(10))

# Estimate the null model (a single rate parameter for the entire tree)
```

```

null <- rate.mult(tree = s$tree, Y = s$Y_means)

# Set 2 groups of species to test for different evolutionary rates
groups <- setNames(factor(c(rep("a",25),rep("b",25)),levels=c("a","b")),s$tree$tip.label)

# Test the hypothesis of different evolutionary rates for each group
compare.rate.mult(rate.mult.fitted = null,groups = groups)

```

sim.curves

Simulate function-valued curve evolution

Description

This function simulates evolution of a function-valued trait (glm with logit link) under Brownian motion.

Usage

```
sim.curves(nspecies = 30, x_length = 20, startree = FALSE, lambda = 1, seed)
```

Arguments

nspecies	Number of species
x_length	Number of points on the curve to simulate
startree	Simulate using a star tree
lambda	Pagel's lambda tree transformation parameter (lambda = 0 for star tree; lambda = 1 for original tree)
seed	Optional seed to set for reproducibility

Value

data	Data frame with simulated curves formatted appropriately for phylocurve()
tree	Phylogenetic tree of class "phylo"
true_coefs	True tip and ancestral coefficients for glm logit link

References

Pagel, M. 1999. "Inferring the historical patterns of biological evolution". Nature 401:877-884.

Examples

```

require(phytools)

# simulate evolution of a function-valued trait (glm with logit link)
sim_data <- sim.curves()

# perform ancestral curve reconstruction
anc_recon <- phylocurve(y~x,tree = sim_data$tree,data = sim_data$data)

# get tip coefficients and aligned function data
tip_coefficients <- get_tip_coefficients(formula = y~x,tree = sim_data$tree,data = sim_data$data)

```

```

data <- get_aligned_function_data(tip_coefficients)

# estimate evolutionary rates
rate.mult.fitted <- rate.mult(sim_data$tree,data)

# estimate phylogenetic signal
K.mult(rate.mult.fitted = rate.mult.fitted)

```

sim.mult *Simulate multivariate trait evolution*

Description

Simulates multivariate trait evolution

Usage

```

sim.mult(nspecies, R, error, nreps = 1, nmissing = 0,
model, parameters, anc, tree, seed, nsims = 1)

```

Arguments

nspecies	Number of species to simulate
R	Covariance matrix for traits to simulate
error	Vector of variances to simulate within-species variation for each trait
nreps	Number of replicates to simulate for each trait per species
nmissing	Number of data points to randomly remove
model	Model of evolution (if not "BM", can be "OUrandomRoot", "OUfixedRoot", "EB", "lambda", "kappa", or "delta")
parameters	List of evolutionary model parameters. For either OU model, use alpha. For EB, use rate. For lambda, kappa, or delta, use lambda, kappa, or delta.
anc	Vector of ancestral values for each trait (default is 0).
tree	Can provide phylogenetic tree for simulations here; otherwise it is randomly generated based on nspecies
seed	Whether or not to set a seed for reproducible results
nsims	Number of simulations (default is 1)

Value

Y_means	Means of simulated data
Y_raw	Raw simulated data (only different from means if nreps>1)
Y_array	Means of simulated data in array format
Y_original	Original simulated species means (only different if nreps>1)
tree	An object of class phylo
tree_sim	The tree on which data was simulated (only different if model!="BM")

Author(s)

Eric W. Goolsby

Examples

```
# Simulate random data for a multivariate trait with 50 species and 10 trait dimensions  
s <- sim.mult(nspecies = 50,R = diag(10))
```

```
# Estimate evolutionary rates  
rate.mult.fitted <- rate.mult(tree = s$tree,Y = s$Y_means)
```

```
# Estimate multivariate phylogenetic signal  
K.mult(rate.mult.fitted = rate.mult.fitted)
```


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